Probing the first stars and black holes in the early Universe with the Dark Ages Radio Explorer (DARE)

Jack O. Burns a,b,* J. Lazio c,b, S. Bale d,b, J. Bowman e,b, R. Bradley f,b, C. Carilli g,b, S. Furlanetto h,b, G. Harker a,b, A. Loeb i,b, J. Pritchard i,b

a Center for Astrophysics and Space Astronomy, Department of Astrophysical and Planetary Sciences, 593 UCB, University of Colorado Boulder, Boulder, CO 80309, USA
b NASA Lunar Science Institute, NASA Ames Research Center, Moffett Field, CA 94035, USA
c Jet Propulsion Laboratory, California Institute of Technology, MIS 138-308, 4800 Oak Grove Dr., Pasadena, CA 91109, USA
d Space Sciences Laboratory, University of California at Berkeley, Berkeley, CA 94720, USA
e Arizona State University, Department of Physics, P.O. Box 871504, Tempe, AZ 85287-1504, USA
f National Radio Astronomy Observatory, 520 Edgement Road, Charlottesville, VA 22903, USA
g National Radio Astronomy Observatory, P.O. Box O, 1003, Lopezville Road, Socorro, NM 87801-0387, USA
h University of California at Los Angeles, Department of Physics and Astronomy, Los Angeles, CA 90095-1547, USA
i Center for Astrophysics, 60 Garden St., MS 51, Cambridge, MA 02138, USA

Abstract

A concept for a new space-based cosmology mission called the Dark Ages Radio Explorer (DARE) is presented in this paper. DARE’s science objectives include: (1) When did the first stars form? (2) When did the first accreting black holes form? (3) When did Reionization begin? (4) What surprises does the end of the Dark Ages hold (e.g., Dark Matter decay)? DARE will use the highly-redshifted hyperfine 21-cm transition from neutral hydrogen to track the formation of the first luminous objects by their impact on the intergalactic medium during the end of the Dark Ages and during Cosmic Dawn (redshifts \( z = 11–35 \)). It will measure the sky-averaged spin temperature of neutral hydrogen at the unexplored epoch 80–420 million years after the Big Bang, providing the first evidence of the earliest stars and galaxies to illuminate the cosmos and testing our models of galaxy formation. DARE’s approach is to measure the expected spectral features in the sky-averaged, redshifted 21-cm signal over a radio bandpass of 40–120 MHz. DARE orbits the Moon for a mission lifetime of 3 years and takes data above the lunar farside, the only location in the inner solar system proven to be free of human-generated radio frequency interference and any significant ionosphere. The science instrument is composed of a low frequency radiometer, including electrically-short, tapered, bi-conical dipole antennas, a receiver, and a digital spectrometer. The smooth frequency response of the antennas and the differential spectral calibration approach using a Markov Chain Monte Carlo technique will be applied to detect the weak cosmic 21-cm signal in the presence of the intense solar system and Galactic foreground emissions.

Keywords: Cosmology: first stars, dark ages, reionization; Radio lines: general; Instrumentation: detectors

1. Introduction

“What were the first objects to light up the Universe, and when did they do it?” These are among the most fundamental questions in modern astrophysics and cosmology as stated recently by the Astro2010 Decadal report, New Worlds, New Horizons in Astronomy and Astrophysics (NRC, 2010). The birth of the first stars and black holes – the end of the Dark Ages or Cosmic Dawn – is a transformative event in the history of the Universe. This epoch provides the key connection between telescopic images of the structures and galaxies seen at redshifts \( z < 5 \) and observations of the extraordinarily smooth Universe 400,000 years after...
the Big Bang ($z \sim 1100$) seen via the Cosmic Microwave Background (e.g., Samtleben et al., 2007). In this paper, we describe a mission concept called the Dark Ages Radio Explorer (DARE) that will investigate this early epoch of the Universe ($\sim 80-420$ million years after the Big Bang) which was heretofore unobservable. DARE will produce the first sky-averaged, low frequency radio ($40-120$ MHz) spectrum arising from the highly redshifted 21-cm signal of neutral hydrogen that uniquely measures the times when the first stars and black holes appeared in the Universe.

These observations are challenging because the expected 21-cm signal strength is considerably below that of several foreground signals. However, DARE eliminates the most intense foreground, namely human-generated radio frequency interference (RFI), by being in a lunar orbit that takes it into the shielded zone above the lunar farside. Science data are acquired only when DARE is above the lunar farside, which is the only location in the inner solar system proven to be free of RFI by Radio Astronomy Explorer-2 (RAE-2, Alexander and Kaiser 1976).

This concept draws on a rich science and technology heritage from a ground-based pathfinder, the Experiment to Detect the Global Epoch of Reionization Signal (EDGES, Bowman and Rogers 2010a). Further, there is a long history of space-based RF systems operating in or near the DARE frequency range, e.g., the Earth remote sensing satellites FORTE, the GeoSAT Follow-On (GFO), and the lunar-orbiting RAE-2 (Alexander and Kaiser 1976).

In this paper, the theoretical drivers, a description of the Science Instrument, and the calibration of the radiometer in the presence of intense foregrounds are presented. The theoretical predictions of the sky-averaged spectrum corresponding to the epoch of the first stars, the first black holes, and the beginning of reionization are described in Section 2. In Section 3, we discuss why observations above the radio-quiet lunar farside are ideal to achieve the first detection of the weak, redshifted 21-cm signals. In Section 4, the DARE radiometer system consisting of tapered bi-conical dipole antennas, a low frequency receiver, and a digital spectrometer is outlined. In Section 5, the calibration and removal of intense cosmic foregrounds is described using differential spectral radiometry. In Section 6, constraints on the epochs of first star and black hole formation from the proposed DARE observations are presented. In Section 7, we conclude with a summary of the DARE mission concept.

2. Theoretical motivation

2.1. Tracing the first luminous objects with the sky-averaged 21-cm spectrum

The Big Bang produced a hot, dense, nearly homogeneous Universe. As the Universe expanded and cooled, particles, then nuclei, and finally atoms formed. At a redshift of about 1100, equivalent to about 400,000 years after the Big Bang, when the primordial plasma filling the Universe cooled sufficiently for protons and electrons to combine into neutral hydrogen atoms, the Universe became optically thin whereby photons from this early era no longer interacted with matter. We detect these photons today as the cosmic microwave background (CMB). The CMB shows that the Universe was still remarkably smooth and uniform, with fluctuations in the mass density of only a few parts in $10^5$ (Hu, 2008). The Cosmic Background Explorer (COBE), the Wilkinson Microwave Anisotropy Probe (WMAP), and a number of ground-based telescopes have mapped this era with extraordinary precision, providing a detailed understanding of this early phase of the Universe’s history (e.g., Dunkley et al., 2009).

After the protons and electrons combined to produce the first hydrogen atoms, the Universe consisted of a nearly uniform, almost completely neutral, intergalactic medium (IGM) for which the dominant matter component was hydrogen gas. With no luminous sources present, this era is known as the Dark Ages. Theoretical models predict that, over the next few hundred million years, gravity slowly condensed the gas into denser and denser regions, within which the first stars eventually appeared, marking Cosmic Dawn, at a redshift $z \approx 30$ (Bromm and Larson, 2004). As more stars formed, and the first galaxies assembled, they flooded the Universe with ultraviolet photons capable of ionizing hydrogen gas. A few hundred million years after Cosmic Dawn, the first stars produced enough ultraviolet photons to ionize essentially all the Universe’s hydrogen atoms (Furlanetto et al., 2006, and references therein). This Reionization era is the hallmark event of this early generation of galaxies, marking the phase transition of the IGM back to a nearly completely ionized state, which is now known to be well underway and potentially nearing completion at a redshift $z \approx 6$ (Fan et al., 2006).

The beginning of structural complexity in the Universe constituted a remarkable transformation, but one that we have only just started to investigate observationally. Existing instruments (e.g., Hubble Space Telescope or HST) show a host of galaxies filling the Universe from about 500 million years after the Big Bang to the present day (i.e., $z < 10$, Bouwens et al., 2011). Interestingly, although these galaxies appear many times smaller than those at lower redshifts, their stellar populations are fundamentally the same, though enriched to a lower level of heavy elements (e.g., McLure et al., submitted for publication). By pushing even farther back, the truly first structures in the Universe can be studied. Theoretical models suggest that existing measurements (from HST and WMAP) are beginning to probe the tail end of Reionization, and the James Webb Space Telescope (JWST) will observe some of the earliest galaxies, possibly out to $z \sim 15$ (Windhorst et al., 2006), while the Atacama Large Millimeter Array (ALMA) will trace the molecular content of galaxies possibly to $z \sim 10$ (Carilli et al., 2008). Even so, the first stars and galaxies – in
the Dark Ages and the Cosmic Dawn – currently lie beyond our reach.

The measurement approach adopted by DARE is to track the influence of the first stars and first accreting black holes on the neutral IGM by means of the intensity of the hydrogen hyperfine (or “spin–flip”) transition. This transition originates from magnetic moments or spins of the proton and electron – if the angular momenta are aligned, the atom lies at a slightly higher energy than if they are anti-aligned (Furlanetto et al., 2006). The energy difference corresponds to a photon of rest wavelength of 21 cm or a rest frequency of 1420 MHz. Because of the expansion of the Universe, these photons from earlier epochs in the Universe are “redshifted” (z) to lower frequencies, νobs = 1420/(1+z) MHz (e.g., at z = 30, ν = 45 MHz). Importantly, the redshifting of the photons allows us to examine the history of the Universe as a function of time (each frequency corresponds to a different redshift or epoch of the Universe). Consequently, observations of the spin-flip line allow the Dark Ages and Cosmic Dawn – when the IGM was mostly neutral hydrogen – to be probed. Moreover, the 21-cm signal complements probes of other telescopes (e.g., HST, JWST, ALMA), as it provides an indirect measure of the effects of distant galaxies on the IGM. This allows it to measure the properties of stars and black holes inside galaxies that are much too small to be imaged directly.

Ground-based low-frequency radio telescopes operating at ν > 100 MHz, such as the Experiment to Detect the Global Epoch of Reionization Signal (EDGES, Bowman and Rogers, 2010), the Murchison Widefield Array (MWA, Onsdale et al. 2009), the Precision Array to Probe the Epoch of Reionization (PAPER, Parsons et al. 2010), and the Low Frequency Array (LOFAR, Harker et al. 2010) will study the end of Reionization. Table 1 summarizes on-going ground- and space-based work and compares these to DARE. Clearly, DARE will probe the redshifted 21-cm signal of hydrogen at higher redshifts (z < 35), where the earliest signals produced by the first stars and accreting black holes, as well as the first stages of reionization, are expected to occur.

Throughout this paper, we use the radio astronomy convention relating power measured by a detector P to a brightness temperature T_b:

\[ P = k_B T_b \Delta \nu, \]

where \( k_B \) is Boltzmann’s constant and \( \Delta \nu \) is the frequency bandwidth over which the measurement is made. The 21 cm background signal brightness temperature is (Madau et al., 1997; Furlanetto et al., 2006):

\[ T_b = \frac{25 x_{HI}}{1 + z} \left( \frac{1 + z}{10} \right)^{1/2} \left( 1 - \frac{T_{CMB}}{T_s} \right) \text{mK}, \]

Here, \( x_{HI} \) is the fraction of hydrogen that is neutral (because spin-flip radiation only comes from neutral gas, \( z \) is the redshift being probed, \( T_{CMB} \) is the temperature of the CMB photon blackbody, and \( T_s \) is the “spin temperature” of the gas. The spin temperature is a measure of the excitation state of the gas, providing the ratio of level populations for the ground and excited states in this transition (with the ground state more highly populated if the spin temperature is small). Its amplitude, and hence the strength of the 21-cm spectral line, depends on the balance between three competing processes: atomic collisions, absorption of CMB photons (and stimulated emission from that photon field), and the ultraviolet radiation background, which in turn reflect processes related to the origin of stars and accreting black holes. Over the redshift range of interest, this last factor contains most of the physical information that DARE will measure. Fig. 1 shows a model for the sky-averaged, redshifted 21-cm spectrum during the Dark Ages, with the brightness temperature measured relative to the CMB (Pritchard and Loeb, 2010, see also Furlanetto, 2006). The brightness temperature evolves with redshift, with several key Turning Points (i.e., inflection points) predicted in the spectrum. These Turning Points mark important physical events (Fig. 1), which are due to the interplay between the first luminous sources and the physics of the hydrogen gas. In the following sections, we summarize the various physical effects that produce the Turning Points, following the approach of Pritchard and Loeb (2010). We stress that the physical processes themselves are based on well understood physics (e.g., quantum mechanics), but their timing and the rate at which they occur (or the resulting strength of the 21-cm signal) are quite uncertain. Thus, observations are crucial to constrain these important events during this epoch.

### 2.2. DARE’s key science questions

The key physical quantities that DARE can measure in order to test this hypothesis are described below in the

<table>
<thead>
<tr>
<th>Telescope</th>
<th>Feature probed</th>
<th>Redshifts</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>HST/JWST</td>
<td>Stellar population</td>
<td>&lt;10 (HST)–15(JWST)</td>
<td>Optical/IR</td>
</tr>
<tr>
<td>ALMA</td>
<td>Molecular gas</td>
<td>&lt;10’’</td>
<td>Millimeter/submm</td>
</tr>
<tr>
<td>LOFAR</td>
<td>Hydrogen/end of EoR</td>
<td>6–11</td>
<td>120–200 MHz</td>
</tr>
<tr>
<td>MWA</td>
<td>Hydrogen/end of EoR</td>
<td>6–16</td>
<td>80–240 MHz</td>
</tr>
<tr>
<td>PAPER</td>
<td>Hydrogen/end of EoR</td>
<td>6–13</td>
<td>100–200 MHz</td>
</tr>
<tr>
<td>EDGES</td>
<td>Hydrogen/end of EoR</td>
<td>&lt;13</td>
<td>100–200 MHz</td>
</tr>
<tr>
<td>WMAP/Planck</td>
<td>CMB</td>
<td>≈1100</td>
<td>22–90 GHz</td>
</tr>
<tr>
<td><strong>DARE</strong></td>
<td>Hydrogen/first stars</td>
<td>11–35</td>
<td>40–120 MHz</td>
</tr>
</tbody>
</table>

similar to those galaxies at CMB. The model assumes that the properties of galaxies at $z$ galaxies. (For interpretation of the references to colour in this figure features marked. $T_E < 0$ is absorption and $T_E > 0$ is emission, relative to CMB. The model assumes that the properties of galaxies at $z > 10$ are similar to those galaxies at $z < 10$. Turning Points (A–E) mark the influence of various events on the neutral intergalactic medium, as traced by the 21-cm hydrogen line and as discussed in more depth in the text. DARE constrains the positions of the Turning Points (B, C, D) and provides the first observational constraints on the first generations of galaxies. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

context of the simple reference model presented in Fig. 1, which is a “best guess” for the physics of these early galaxies given current information. We will also describe the wide range of plausible variations still allowed by theoretical models and how they influence the signal. We stress again that our summary reflects the current best understanding of this era, but this understanding is derived entirely from theoretical models. DARE’s objective is to provide an observational basis for these discussions.

2.2.1. When did the first stars ignite?

Before the first stars and galaxies formed, the hydrogen gas was influenced only by atomic collisions, absorption of CMB photons, and gravitational effects. The gas cooled rapidly as the Universe expanded, to the point that the spin temperatures were lower than that of the CMB. At sufficiently early times, the high gas density caused a large rate of atomic collisions, so that the spin temperature approached the gas temperature, causing the 21-cm signal to appear in absorption against the CMB. However, as the Universe expanded, the decreased gas density reduced the collision rate, and interactions with CMB photons drove the spin temperature back into equilibrium with the CMB. This caused the spin-flip absorption signal to decrease and eventually disappear by $z \sim 30$ (between Turning Points A and B), because there is no longer any relative absorption or emission against the CMB.

Current predictions are that, shortly thereafter, the first stars appeared ($z \sim 30$, Turning Point B). Their ultraviolet photons scattered throughout the intergalactic medium and “turned on” the spin-flip 21-cm signal through the so-called Wouthuysen–Field mechanism (Wouthuysen, 1952; Field, 1959). Photons that redshift into the Lyman-$
\alpha$ transition of neutral hydrogen cause the electron to jump from the ground state to the first excited level, from which they rapidly decay back to the ground state. However, the quantum mechanical selection rules allow the electron to occupy a different hyperfine state after this excitation and decay than before. When enough such scatterings occur, these interactions determine the spin temperature and bring it back into equilibrium with the gas temperature (still much colder than the CMB). Thus, the first stars produced a deep absorption trough (between Turning Points B and C, e.g., Furlanetto et al., 2006).

By determining the redshift of this transition, DARE will make the first measurement of the onset of star formation in the Universe. Interestingly, theoretical models predict that these stars form very differently than those near Earth: without heavy elements, the chemistry of this primordial gas differs from that in later generations of galaxies, likely causing the first stars to be tens or even hundreds of times larger than nearby stars (Bromm and Larson, 2004). Observational probes of these first luminous objects are essential for understanding these first phases of structure formation.

Equally interesting is the transition from these exotic stars to more normal stars, which depends on several poorly-understood feedback mechanisms, like chemical enrichment, supernova feedback, and the ultraviolet radiation field (e.g., Furlanetto et al., 2006). This transition determines the slope at which the absorption deepens, between Turning Points B and C (Fig. 1), and DARE’s measurement will provide a robust measurement of the radiative feedback in particular (Holzbauer and Furlanetto, submitted for publication).

Fig. 2 illustrates the sensitivity of the spin-flip 21-cm signal to the ultraviolet radiation of the first stars. The solid black curve is identical to the model in Fig. 1, but the blue curves vary the ultraviolet luminosity of the first stars by a factor of 100. Measuring the redshift of Turning Point B, and the shape of the subsequent absorption trough between Turning Points B and C, therefore constrains the formation mechanism of these stars and their properties.

2.2.2. When did the first accreting black holes form?

Black holes likely formed shortly after the first stars. Their intense gravity would have strongly accelerated any gas falling onto them, shock heating it to high temperatures and inducing strong X-ray emission. In contrast to ultraviolet photons, which have an extremely small mean free path into neutral hydrogen gas, X-ray photons can penetrate to great depths, but they eventually scatter through
The nature of the first black holes remains even more of a mystery than the first stars, forming either as ~10–100 solar mass remnants from those stars’ explosions (e.g., Volonteri et al., 2008) or in much larger seeds (up to ~10,000 solar masses) via the direct collapse of gas in unusual environments where star formation was ineffective (Bromm and Loeb, 2003). In either case, they must have accreted material very quickly in order to produce the ultra-luminous “quasars,” powered by accretion into black holes a billion times more massive than the Sun, that are visible as early as 1 billion years after the Big Bang (Fan et al., 2006). The growth of these black holes determines the slope of the DARE spectrum between Turning Points C and D, during which the signal passes from absorption into emission as the gas became hotter than the CMB (between Turning Points C and D). Thus, by measuring the onset of gas heating at Turning Point C, DARE detects the earliest evidence of black hole accretion in the Universe.

The red curves in Fig. 2 show how the spin-flip signal varies the X-ray heating rate by a similar factor. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
the signal is affected in some such alternate scenarios. For illustrative purposes, we consider several different scenarios here (see also, e.g., Furlanetto et al., 2006; Mack and Wesley 2008; Natarajan and Schwarz 2009). The red line shows the signal if an unknown radiation background heats the intergalactic gas to high temperatures and couples the spin temperature to it. The dashed line shows a model in which dark matter annihilates over a long time scale, heating the gas significantly. The blue line shows a model without an ultraviolet background, rendering the Wouthuysen–Field mechanism ineffective and the spin-flip line nearly invisible. Finally, the dotted line turns off X-ray heating, allowing the IGM to remain cold and visible in strong absorption.

While all of these examples seem implausible today, they illustrate the power of exploring an entirely new era within the Dark Ages. By observing in this previously unexplored redshift range, DARE can confirm current models of the first luminous objects or measure deviations from models that might illuminate new physics.

3. Why DARE needs to orbit the Moon

A significant hurdle to a terrestrial global 21-cm experiment is human-generated RFI. Our civilization emits the vast majority of its integrated radio power at DARE frequencies (Loeb and Zaldarriaga, 2007). At the Murchison Radio Observatory in Western Australia, a government-protected site, several FM radio signals are persistently detected by EDGES at the 1 K level (1000 times the limit needed to detect the Turning Points in Fig. 1) due to reflections from meteors and aircraft (Bowman et al. 2008; Rogers and Bowman 2008; Bowman and Rogers 2010a,b; EDGES memo series1). Reflections from density structures in the ionosphere are also possible (Lazio et al., 2010).

In low Earth orbit (LEO), the effective antenna temperature from a single terrestrial FM transmitter in direct line-of-sight to the spacecraft could exceed $10^4$ K in a 1 MHz spectral channel, as compared to the 1 mK limit that we require for science observations (see Section 4). In geosynchronous Earth orbit (GEO), the effective antenna temperature would be reduced to only $\sim 10^3$ K. At the lunar L2 Lagrange point, $\sim 60,000$ km behind the Moon, the solar disk does not sufficiently occult the Earth, because of diffraction of radio waves around the lunar limb. A distance of at least 4 AU is required to prevent DARE from detecting terrestrial RFI above 1 mK.

An alternate approach would be to equip the DARE spacecraft with a metallic screen designed to shield the spacecraft, and the science instrument, from terrestrial RFI. This approach would be analogous to the Sun shield planned for JWST. While such an RFI shield is in principle possible, e.g., achieving 50 dB of shielding, diffraction about the shield would still result in an effective antenna temperature of 4000 K if DARE were in LEO and 200 K at the lunar L2 point. Further, such a shield would be massive (increasing launch costs) and almost certainly require deployment, thereby increasing mission risk.

Lunar orbit is a far more practical solution. Further, both RAE-2 and the Apollo Command Modules, which had RF systems that bracket, DARE frequencies, observed complete cessation of terrestrial RF emission when they passed into the radio-quiet zone above the lunar farside. Finally, reflections of terrestrial RFI from other spacecraft in view of DARE while in the radio quiet zone will be at a negligible level (<1 nK). Placing DARE above the farside of the Moon removes all complications from Earth’s ionosphere and terrestrial RFI, and blocks heliospheric emissions from the Sun for part of the orbit.

DARE’s position behind the Moon opens the entire RF spectrum to astronomical use, simplifies the receiver design, improves its inherent performance, and enables the science objectives. Completely eliminating RFI (from the Earth and the spacecraft environment) is the only guarantee that the redshifted 21-cm signal will not be corrupted by uncharacterized spectral artifacts. By lowering the spectral dynamic range from $>10^9$ to the sky limit of $10^6$, DARE avoids the bit-depth, linearity, clock stability, and digital noise challenges experienced by ground-based experiments.

---

DARE provides an ideal environment for the science antenna. The potential for far-field scattered radiation and uncertainties in the operational conditions are greatly reduced, allowing for the antenna impedance and primary beam pattern to be more stable, accurately modeled, effectively calibrated, and better matched to science goals. Control and characterization of antenna properties are the most important factors for subtracting astronomical foregrounds (Sections 4.4 and 5).

Finally, the motivation for DARE parallels the successful history of cosmic microwave background (CMB) anisotropy experiments. CMB studies are accomplished from the ground or balloons, but the space environment substantially improves scientific return. Terrestrial CMB instruments including BOOMERANG, DASI, CBI, and others developed fundamental techniques and illuminated key scientific uncertainties, but space missions COBE, WMAP, and Planck have capitalized on the space environment to provide definitive measurements. DARE builds on ground-based heritage, uses the ideal properties above the lunar farside to eliminate RFI, and provides a well characterized science antenna in order to achieve the best possible measurement of the redshifted 21-cm global signal.

4. The DARE radiometer

The DARE science objectives require a carefully calibrated, load switching radiometer to measure radio frequency (RF) spectra over the 40–120 MHz range (Fig. 4) of the VHF band. This radiometer consists of a dual-polarized antenna with a compact, integrated, front-end electronics package, a single-band, dual-channel receiver, and a digital spectrometer. The heritage of VHF band radiometry spans a half-decade to include ground-based experiments such as EDGES and PAPER, Earth remote sensing satellites like FORTE and GeoSAT Follow-On (GFO), and lunar orbiting spacecraft such as the Radio Astronomy Explorer-2 (Explorer 49). While the specific design of the DARE instrument is new, all subsystem components have a strong heritage with a technology readiness level (TRL) of at least 6 (TRL ≥ 6) on the standard scale.

To extract the desired science results at the significance levels described in Section 2, the radiometer must be well calibrated (Section 4.5). The DARE instrument design is guided by years of experience in calibrating spacecraft radiometers such as AMR and ground-based experiments such as EDGES and PAPER. Challenges addressed by the design include adequately characterizing the antenna power pattern, understanding the receiver noise contributions, and maintaining sufficient linearity to extract the 21-cm spectral features in the presence of dominant foregrounds.

Sensitive radiometers require that all supporting subsystems, including everything from Command and Data Handling (CDH) to the power supplies, must be RFI-quiet so as not to adversely affect the science measurements. However, two additional requirements are imposed on the DARE radiometer: (1) the system must be stable enough to permit long-duration, statistical measurements over many months of observing, and (2) the spectral response is smooth so that residual features upon calibration are small enough to permit unambiguous, noise-limited localization of the Turning Point frequencies. These special requirements together with the additional constraint that the science instrument will only operate when the spacecraft is above the lunar farside, makes DARE a rather novel radiometer system.

4.1. Science requirements

The design of the DARE radiometer, from the RF transfer characteristics to the data management rates and operational features, is driven by the basic science requirements. In this section, we summarize only those RF characteristics that affect the science measurements. These include frequency range, spectral resolution, spectral response, and sensitivity.

4.1.1. Frequency range

This requirement is set specifically by the goal of measuring the redshifts at which Turning Points B, C, and D occur. Current theoretical models suggest that these Turning Points should occur over the approximate redshift range of 11–35. Given the relation between rest-frame and observed frequency, this redshift range translates to a frequency range of 40–120 MHz, which is the design requirement for the Radiometer. We have not attempted to measure the redshift of Turning Point E because there are ground-based instruments that are likely to constrain the properties of the intergalactic medium at the end of the Epoch of Reionization before or on the same time scale as DARE becomes operational. Early in the concept development phase, we decided not to attempt to measure the redshift of Turning Point A because the mission duration would be excessively long. We discuss foregrounds and sensitivity below, but, briefly, at lower frequencies, foregrounds become stronger, necessitating ever longer mission durations.

4.1.2. Spectral resolution

This requirement is set by the characteristic scale over which the Turning Points occur. Current theoretical
models suggest that a useful measure would be 1 MHz. However, recombination lines from carbon atoms have been detected within or just below the DARE frequency range. These recombination lines are much narrower than 1 MHz. Estimates of their amplitude are uncertain as they depend upon the poorly known distribution of recombination line hosting gas within the Galaxy. Nonetheless, it is possible that recombination lines could produce a signal comparable to that expected for the Turning Points (Peters et al., 2011). In order to have sufficient spectral resolution to identify, and possibly mask recombination lines during the analysis, we specify a requirement of 10 kHz.

4.1.4. Sensitivity

This requirement is set by the expected amplitudes of the Turning Points and the need to have an adequate signal-to-noise ratio. As can be seen from Fig. 1, the amplitudes, relative to the CMB, vary for the different Turning Points. We adopt a value of 1 mK, in a 1 MHz band, as the sensitivity requirement, with this value being constant across the DARE frequency range. This value should provide a high signal-to-noise ratio detection for Turning Points C and D and should be adequate to identify the location of Turning Point B (see Section 5). Indeed, even if Turning Point B lies outside of the DARE frequency range, with this sensitivity requirement, we would still be able place some constraints on Turning Point B’s location by using the shape of the measured spectrum.

4.2. Antenna

The key trades for the antenna design were among mass, volume, and electrical performance. A bi-conical dipole is a compact and low mass structure, yet also achieves the electromagnetic performance specified by the science requirements (Section 4.1). Alternate topologies such as high gain, aperture-type configurations and log-periodic antennas were excluded on the basis of their large size, the strong dependency of their terminal impedance on frequency, or both.

An electrically short dipole (<0.6λ) will be used, with the half-wavelength resonance designed to occur near the upper end of the band. Consequently, the power pattern remains symmetrical, and both it and the terminal impedance should vary smoothly with frequency; the overall gain is lower than that of a resonant dipole but is sufficient given the strong Galactic emission at these frequencies. The combination of large diameter and tapering (1) lowers the dipole’s Q (quality factor) to increase its bandwidth; (2) reduces reactive effects due to the series inductance at the end of the arm or arm-to-arm capacitance across the feed terminals; and (3) pushes any resonances due to circuit parasitic effects across the antenna terminals above the 40–120 MHz range.

The dipole cones will be constructed from an internal wire frame covered with standard gold-plated wire mesh used on deployable communication antennas. The dielectric support will be an Astroquartz/Kevlar fiber and cyanoate ester resin composite, which has good thermal stability, low RF loss, and has heritage from Deep Impact and the Mars Exploration Rovers (MER) (Fig. 5). Further, this dielectric support will have a high resistivity, RF transparent Ge coating in order to bleed off any solar wind induced charge.

To improve the antennas’ electrical performance, an effective ground plane will be formed by deployable cylindrical radials extending outward from the spacecraft body and located approximately a quarter-wavelength (at the resonant frequency) from the dipole plane. The radials increase the forward gain, thereby (1) limiting the spatial extent of the sky model needed for calibration; (2) reducing the effect of...
asymmetrical spacecraft structures; and (3) providing modulation in detected power with spacecraft orientation. Radials are used to eliminate the need for a large monolithic structure, which would pose a significant deployment challenge. By contrast, small-diameter metallic radials can function as an effective ground plane, providing about 15 dB front-to-back ratio for 24 radials and have been deployed in hundreds of space missions without a single failure.

Modeling of the antenna indicates that it can be characterized to the level required to meet the science objectives and as specified by the science requirements. That is, its frequency response can be captured to very high precision by a simple parametrized model, the parameters of which are fit simultaneously with the parameters of the foregrounds and the cosmological signal by the MCMC code described in Section 5 (for more details, see Harker et al., 2011). These parameters do not have to be determined to the final required accuracy from simulations or pre-launch measurements, since they can be constrained by the science data themselves. Rather, the pre-launch measurements provide guidance as to the form of the parametrized model, and some prior information on its parameters.

The electromagnetic performance of the antenna, radials, and a hexagonal spacecraft were modeled using CST Microwave Studio. Each dipole arm is 59 cm in length, with a taper of 40° to provide a smooth instrument response, and an 8.3° rotation away from the spacecraft to accommodate the likely launch vehicle fairing. The terminal ends are 65 cm from the 24 ground radials, each of which extends 2 m from the spacecraft. The model also included (1) a cylindrical mast and a metal conduit running from the spacecraft to the dipole feed points; (2) non-conductive support structures near the ends of the arms; (3) the front-end electronics; and (4) the propellant tank at the ground plane.

The power pattern is a single-lobed, smoothly varying spatial function (Fig. 6), and the minimum directivity occurs off the ends of the dipole arms. The terminal impedance follows a well-behaved function of frequency, varying smoothly from 40 to 120 MHz (Fig. 8). The gain ranges from 6.2 dBi at 40 MHz to 7.2 dBi at 100 MHz then dropping back to 6.0 dB at 120 MHz.

A change in the dimensions of the antenna caused by thermal expansion will influence the resonant frequency of the dipole. The antenna’s gain (beam pattern) and its terminal impedance will be affected, but the extent that this influences the calibration of the radiometer is mitigated by the wide operational bandwidth of a bi-conical dipole, which effectively lowers the quality factor ($Q$) of the resonator. The frequency response function of the bi-conical, whose small scale structure is on the order of many ten’s of MHz, will only be shifted by a few kHz without introducing new structure. This effect was modeled using the MCMC code described in Section 5 and was found to have only a small effect on the calibration, increasing the errors on the turning points by only 5–10%. The pointing of the beam will not be affected if the expansion is symmetrical. However, the pattern is also quite broad in extent and, as such, a small asymmetry in the expansion will result in a pointing offset that is a tiny fraction of the beamwidth, thus resulting in an imperceptible change in pointing.

4.3. Receiver

The DARE receiver (Fig. 7) provides amplification of the antenna signal to a level sufficient for further processing by the Digital Spectrometer and incorporates a load switching scheme to assist calibration. There are two receivers to accommodate the Science Antennas – one per antenna polarization. The front-end electronics will reside within the central mast of the dipole structure so that the amplifiers can be placed in close proximity to the Antenna to ensure the simplest possible interconnection. This strategy is based on EDGES’ experience, with the goal of minimizing the complexity of the receiver noise model, especially with regards to spectral artifacts that would otherwise be introduced by longer cables and other reactive elements between the Antenna and amplifier.

Load switching is at the core of differential radiometry. In the DARE receiver, the switching is performed directly after the first stage low noise amplifier (LNA). Hence, the two pathways through the switch consist of (1) the antenna followed by an LNA and (2) the load resistor followed by an LNA. The two LNAs form a matched pair sporting nearly identical bandpass behavior. The DARE receiver also incorporates the novel feature where, for a given polarization, each of the two arms or cones of the bi-conical dipole is connected to a separate LNA. The signals exiting the switches are combined by a 180° hybrid coupler to form the output signal. Hence, for the complete dual polarization system, there are two hybrid couplers and four each of the antenna arms, load resistors, matched pairs of LNAs, and RF switches.

Although this circuit configuration appears similar to a Dicke switch for a microwave radiometer, it differs substantially from a conventional load switching radiometer to meet the science objectives. These switches serve primarily as spectral references, and secondarily for temperature.
reflection coefficient (Eq. (3)).

from $C_0$ to $C_1$; ensuring linearity and spectral purity is paramount. By intermodulation of the signal with itself. Again, maintaining against spectral artifacts that would otherwise be produced in single-ended amplifier configurations. This is a precaution and thereby minimizes distortions otherwise present in well-known topology ensures symmetry in the voltage transphases and combining them again after amplification. This further details of the instrument calibration methodology. Noise diodes further down the receiver chain provide a reliable additive noise temperature during operation. These noise diodes will be used to monitor spectral response and linearity of downstream components. The inclusion of these circuits is based on many years of radiometer experience at JPL including the radiometer for the JUNO mission and the advanced microwave radiometer (AMR). By including redundant and independent calibration sources, problems can be quickly detected and diagnosed throughout the development, testing, and operation phases. Section 4.5 discusses further details of the instrument calibration methodology.

The switches will be operated both in tandem and independently to confirm that spectral changes observed in each Antenna are symmetric and uncorrupted by spectral artifacts that may be introduced downstream. By placing the switch after the first LNA, the LNA itself serves as the isolator to keep switch impedance constant throughout the switching cycle. This provides an effective tool to monitor the gain stability of the system. The gain of the system is further ensured by controlling the thermal environment of the front end (discussed below).

Noise diodes further down the receiver chain provide a reliable additive noise temperature during operation. These noise diodes will be used to monitor spectral response and linearity of downstream components. The inclusion of these circuits is based on many years of radiometer experience at JPL including the radiometer for the JUNO mission and the advanced microwave radiometer (AMR). By including redundant and independent calibration sources, problems can be quickly detected and diagnosed throughout the development, testing, and operation phases. Section 4.5 discusses further details of the instrument calibration methodology.

The signal will be amplified further in balanced stages, employing $180^\circ$ hybrids to split the signal into opposing phases and combining them again after amplification. This well-known topology ensures symmetry in the voltage transfer and thereby minimizes distortions otherwise present in single-ended amplifier configurations. This is a precaution against spectral artifacts that would otherwise be produced by intermodulation of the signal with itself. Again, maintaining linearity and spectral purity is paramount.

The spacecraft thermal environment is expected to vary from $-100$ to $+130^\circ$C. If not thermally controlled, gain variations within the Receiver would corrupt the science measurement. Critical front-end components will be packaged in a “cylinder within a cylinder” thermal system, developed and demonstrated at JPL for ground-based and space-borne RF systems, that maintains mK stability. The concept involves placing the front-end electronics within the mast that supports the Antennas. Heat fluxes from the dipole elements are shunted at the base of this assembly, which is actively stabilized with proportional–integral–differential (PID) temperature controllers operating Peltier elements to pump heat downward in two stages – into the mast structure and eventually to spacecraft radiators. The top of the mast structure contains the active (i.e., heat producing) receiver electronics, which are thermally shunted downwards into this same thermal control point. The top enclosure is constructed much as a Dewar, with 3 concentric polished metal cans forming a thermal break. The extremely tight $1$ mK thermal stability is achieved in stages: the outer mast surface will vary by about $30$ K between sunlight and darkness, according to preliminary analysis; the intermediate thermal shunt will vary $\pm 0.1$ K, and the inner electronics by $\pm 1$ mK. The mass within this thermal enclosure is estimated to be $0.1$ kg, and electrical wiring will be thermally shunted to the heat sinks at each control point via heat conducting electrical insulators between each stage.

The remainder of the Receiver will be housed within the spacecraft. Cryogenic cables will act as a thermal break to prevent heat losses from the Receiver enclosure. This type of cable has heritage from deep space, near Earth, and military applications; has superior insertion loss and phase performance throughout a large temperature range; and has a tight bend radius, allowing for ease of assembly. A final stage of amplification will provide sufficient signal amplitude to drive the analog-to-digital conversion in the Digital Spectrometer. Low-pass filtering of the signal also will be performed to prevent aliasing within the Digital Spectrometer.

A (standard) electronics assembly will provide regulated $\pm 12$ V DC power to the front-end assembly. It is important to regulate the voltage externally to the front end so that heat dissipation within the front end is constant with time. An onboard 3-terminal linear regulator will reduce the 12 V
DC to the desired bias voltage with appropriate filtering to minimize bias-related noise. The switches and noise diodes will be biased using separate linear regulators, their control circuitry will be inside the front-end, and the control lines will be activated via opto-couplers to enhance noise immunity. The temperature sensor outputs will have a dedicated connector to minimize noise contributions. The packaging will have sufficient EMI shielding to minimize external influences and prevent any surface charge related incidents.

4.4. Digital spectrometer

The Digital Spectrometer design is driven by requirements to resolve mK level spectral features on smoothly varying backgrounds ranging from about 4000 K at 40 MHz to about 400 K at 120 MHz and to provide a spectral resolution of better than 10 kHz, with excellent channel-to-channel isolation. These requirements are modest by modern standards, as are the resulting data rates.

For the DARE Radiometer, a digital polyphase spectrometer has been adopted. Such spectrometers can be designed to the required bandwidth, resolution, channel shapes, and Analog-to-Digital Converter (ADC) resolution, and can be implemented using a space-qualified FPGA. Jarnot et al. (2011) describes a prototype, including field data.

There are several suitable rad-tolerant ADCs, such as those from National Semiconductor, that implement two ADCs, allowing a dual Digital Spectrometer to be implemented in a single ADC and FPGA device.

There are many FPGA-based digital polyphase spectrometers, with systems potentially able to use either a Xilinx or Actel FPGA. Both are available in a radiation-tolerant form; the Actel implementation offers potentially lower cost, with systems potentially able to use either a Xilinx or Actel FPGA.

FPGAs can also implement a soft-core processor, allowing some C&DH functionality to be included in the spectrometer. This allows a degree of “intelligence” and programmability, e.g., the ability to ignore portions of the spectrum subject to any internal interference and to bin channels intelligently to minimize data rates.

Quantization has, at best, a weak effect on errors for 3-bit digitizers, and substantially less for higher numbers of bits; typical space-qualified ADCs will provide sufficient accuracy to reduce any such errors to an extremely small fraction of the overall error budget. In a terrestrial environment, the most significant impact is from signals with non-thermal noise like statistics such as RFI (e.g., Ferris and Saunders, 2005), which is not an issue for DARE.

4.5. Calibration

The Instrument design is coupled to a multi-tiered calibration strategy to obtain the RF spectra from which the 21-cm signal can be extracted. The calibration strategy relies on the fact that a high degree of absolute calibration is not required, but focuses on the relative variations between spectral channels, which are much easier to control. This multi-tier strategy is based on proven techniques for receiver calibration and augmented by techniques developed during four years of design refinement and thousands of observational hours with EDGES.

4.5.1. Calibration of the antenna–receiver junction

The relative spectral smoothness requirement presents the largest challenge at the Antenna-Receiver interface. Based on EDGES experience, DARE reduces significantly the transmission line length between the antenna and first-stage amplifiers. This arrangement causes any reflected power to create only long-period standing waves that can be fit with a smooth function in frequency.

In a lossless system, the impedance mismatch between the antenna and first-stage amplifiers results in a spectrum of Meys (1978):

$$T_{\text{ant}}(v) = T_{\text{rec}}(v) + |\Gamma(v)|^2 T_b(v) + 2T_b |\Gamma(v)|$$

$$\times \cos(\beta + \phi_\Gamma) + |1 - |\Gamma(v)||^2 T_{\text{sky}}(v),$$

(3)

where $T_{\text{rec}}$ is the noise power that is emitted from the output ports of the amplifiers and $T_b$ is the noise power that propagates from the input port of the amplifiers back to the antenna. $\Gamma$ is the complex reflection coefficient of the antenna due to its impedance mismatch (see Harker et al., 2011 for an example of the DARE antenna reflection coefficient) with the receiver and $\beta$ is the phase of $\Gamma$, resulting from the antenna’s electrical path length and embedded circuitry. $T_c$ and $\phi_\Gamma$ represent the amplitude and phase of the correlated components of the amplifier noise terms, and $T_{\text{sky}}$ is the sky temperature convolved with the antenna beam pattern. The first term in this equation represents the canonical noise propagating directly from the receiver, while the second term is due to the often-neglected amplifier noise reflected back from the antenna. The third term describes the constructive and deconstructive interference between the correlated components of the first two terms, and the final term is the actual sky power propagated into the system through the antenna.

For a broadband instrument such as DARE, the antenna’s impedance varies strongly with frequency and, in general, will not match the receiver’s impedance. However, the antenna impedance can be measured (or modeled) to sufficient accuracy to satisfy the 10% absolute calibration requirement, and the antenna’s compact structure also means the impedance will change slowly with frequency.

Moreover, placing the first-stage amplifiers close to the antenna feeds results in an effective electrical path length of less than 0.1λ between the antenna and amplifiers, making the period of the spectral standing wave much larger than the instrumental bandwidth, and thereby reducing the number of degrees of freedom needed to fit the spectral structure.
4.5.2. Calibration of analog and digital path

The Instrument must achieve a dynamic range exceeding $10^{3}$ in its final integrated spectrum between the average sky noise power and the desired spectral signal (1 mK signal with about a 1000 K foreground), but it only needs to calibrate the absolute power at the 10% level. This dynamic range and absolute calibration precision are regularly achieved in ground-based and space-borne receivers using internally-switched inputs to calibrate the gain and additive noise of the analog and digital receiver path. EDGES demonstrated that this calibration approach, applied in a similar spectral band, can achieve a dynamic range greater than $10^{5}$. Although other instrumental properties dominated the large-scale spectral performance of EDGES in Bowman and Rogers (2010), the measured dynamic range in response to narrow spectral features was limited only by available integration time.

The Instrument follows the traditional internally-switched calibration approach to correct for additive noise and linear gain variations in the receiver path by switching between the antenna feeds and two loads (Fig. 7). Toggling between the loads and the first-stage amplifiers produces a three-state system:

$$
 p_0(v) = g(v)[p_{atten}(v) + p_{amp}(v)],
$$

$$
 p_1(v) = g(v)[p_{load}(v) + p_{amp}(v)],
$$

$$
 p_2(v) = g(v)[p_{ant}(v) + p_{amp}(\mu)],
$$

where $p_0$, $p_1$, and $p_2$ are the spectra from the three input states. Here, $g$ is the collective gain of the amplifiers and filters in the analog path, $p_{atten}$ is the spectrum from an attenuated load, $p_{load}$ is the spectrum from the load without attenuation, $p_{amp}$ is the spectrum from the first-stage LNA, and $p_{ant}$ is the sky spectrum after propagating through the antenna. Using the pre-flight temperature calibration of the noise loads, the three spectra are used to calibrate the antenna temperature:

$$
 T_{ant}(v) = T_{atten}(v) + [T_{load}(v) - T_{atten}(v)][p_2(v) - p_0(v)]/[p_1(v) - p_0(v)],
$$

where $T_{load}$ and $T_{atten}$ are the pre-flight calibrated noise spectra and $T_{ant}$ is the calibrated antenna temperature. Spurious signals produced by the digital electronics cancel through the subtractions in Eq. (5) while the divisions remove the gain contribution $g$.

In the current design, the Instrument cycles between the 3 states on a regular cadence of approximately 60 s during science observations. The resulting spectra are transmitted to the ground data system, which implements Eq. (5) to yield calibrated spectra. Equal time will be spent in each state so that the thermal uncertainty in the final calibrated spectrum is not dominated by a single state.

Pre-flight calibration of the first-stage loads is needed only at 10% to satisfy the absolute calibration requirements. During flight, control and monitoring of the load temperatures ensure that the pre-flight calibration can be applied. A compact, clumped element load was shown by EDGES to provide a suitable, spectrally smooth reference spectrum.

4.5.3. Modulation of the sky

The observing strategy is a final means for precision calibration. By treating Eq. (5) also as a function of spacecraft orientation, $T_{sky}$ becomes dependent on four variables (frequency, roll, pitch, yaw), whereas the instrument-dependent systematic effects remain independent of the spacecraft orientation and only depend on frequency. Spacecraft orientation changes modulate the sky signal by viewing different regions of the Galactic emission. This modulation breaks the degeneracy between the instrumental terms and the sky signal (Eq. (5)) and allows the reflection coefficient and other calibration effects to be fit as model components in a comprehensive analysis of the data time series, much like the approach employed to calibrate many CMB experiments (Section 5). Any orientation-dependent structure in the spectrum that does not correlate with this modulation is isolated in the final processing since it cannot originate from the 21-cm signal.

5. Extracting the cosmic 21-cm signal in the presence of bright foregrounds

Achieving the DARE science objective will be challenging because the redshifted 21-cm signal is only one contribution to the measured RF spectra. The magnitudes of these other contributions (“foregrounds”) exceed that of the 21-cm signal by factors of $10^{5}$–$10^{6}$, depending upon the frequency and position on the sky.

The DARE Science Instrument measures spectra between 40 and 120 MHz. Each spectrum is the sum of three components: the 21-cm signal, foreground radiation, and Gaussian thermal noise. At each time, the magnitude of the foregrounds depends on the direction in which the spacecraft is pointing, being an average of the true sky temperature over the antenna power pattern (Fig. 6). In principle, the power pattern affects the contribution of both the 21-cm signal and the foregrounds, but in practice it is so broad, and thus averages over such a large volume of the high redshift Universe, that the 21-cm signal is constant on the sky at DARE’s resolution. The radiometer modifies the sky spectrum through a frequency-dependent instrument response (Fig. 8), changes the properties of the noise, and potentially introduces spurious spectral features. We have demonstrated via a numerical simulation an effective procedure for extracting the 21-cm signal from these spectra, including all foregrounds and the instrument response, which produces realistic errors (0.5–10%) on the inferred position of the spectral Turning Points. Table 2 summarizes our procedure, and Fig. 9 presents the results. The rest of this Section describes the details behind Fig. 9.

DARE’s antenna power pattern covers approximately 1/8 of the sky, depending on frequency, and consequently we model the DARE data set as consisting of spectra from 8 independent regions on the sky. These spectra are used
Jointly in our maximum likelihood analysis. Parameterized models are used for the foregrounds, 21-cm signal, and instrumental response. These parameters are constrained simultaneously in a Bayesian framework by finding the parameter combination which maximizes the posterior probability of the model parameters given the data. We use the well-established and efficient Metropolis–Hastings algorithm to map out the likelihood. This is a member of a family of Markov Chain Monte Carlo (MCMC, Lewis and Bridle 2002) simulation methods. Given a generative model that predicts the sky brightness as a function of parameters describing the contribution from foregrounds, 21-cm signal, and instrumental response, the MCMC simulation determines the most probable values of the model parameters, and confidence intervals thereon, given DARE’s observations of the sky. This method produces unbiased random samples from the posterior probability distribution, with the density of samples within a given region being proportional to the probability. More likely regions of parameter space have a greater density of points, and an $\alpha$% confidence region is a region with a density of points above a certain threshold, such that the region contains $\alpha$% of the points in the random sample generated by MCMC.

The choice of model parameters is crucial. We must choose a parameterization sufficiently flexible to describe all contributions to the integrated spectra accurately, yet without introducing severe degeneracies between the parameters. The 21-cm signal is parameterized by the frequency and amplitude of Turning Points B, C and D. Fig. 9 illustrates the constraints on these Turning Points from a simulated DARE mission. Fig. 10 shows how uncertainties on these parameters translate into uncertainties on the shape of the recovered 21-cm signal. The different parameter groups are summarized in Table 3, and we describe them in more detail in Section 5.1. In Harker et al. (2011), we present further details on the MCMC methodology applied to the 21-cm sky-averaged signal problem. Harker et al. (2011) describe several tests of the signal extraction technique, for example: contrasting the realistic case for which we show results here with one assuming a perfect instrument; showing the effect of different amounts of integration time; and varying the quality of the assumed prior constraints on instrumental and foreground parameters, which would be obtained from measurements made prior to launch or during calibration observations. By studying the covariance between the signal parameters and the rest, one can also understand how systematic errors in instrumental parameters would feed through into the inferred signal. We do not explore these issues here but, rather, we are focused on what the MCMC simulation can tell us about DARE’s sensitivity to the cosmological signal under our fiducial assumptions about the instrument and the signal.

5.1. Models for the foregrounds and the DARE frequency response

The Turning Point parameterization of the 21-cm signal (parameter group 1 in Table 3) has been described in Section 2. Because each of our eight sky regions covers a very large volume of the Universe at the redshifts of interest to DARE, the 21-cm signal spectrum averages out and is identical in each region, so a total of 6 parameters is required to describe the 21-cm signal. By contrast, the foregrounds are spatially varying, as can be seen in Fig. 11.

Most of the spatial structure apparent in Fig. 11 is synchrotron radiation from the Galaxy and constitutes the dominant foreground, responsible for approximately 73% of the total (Shaver et al. 1999). Synchrotron radiation should vary smoothly in frequency (e.g., Petrovic and Oh, 2011). A second contribution to the foregrounds comes from extragalactic sources. Though these are discrete, the solid angle of the DARE beam is so large that it averages together a large number of sources, so that they can be treated as another diffuse foreground. These sources also have a synchrotron spectrum. A final, small (~1%) contribution to the diffuse foregrounds comes from thermal (free–free) radiation from our Galaxy, which should produce a smooth spectrum. Because of this smoothness, the diffuse foreground spectrum in each sky region can be described using only a small number of parameters. The model used is:

\[ \log T_{FG} = \log T_0 + a_1 \log v + a_2 (\log v)^2 + a_3 (\log v)^3, \]

where \( T_0, a_1, a_2, a_3 \) are the parameters. Higher order polynomials are trivial to incorporate, but Pritchard and Loeb (2010) concluded that this set of parameters was the smallest number of polynomial coefficients needed to describe the spectrum to the required level of accuracy. In general, the parameter values are different in each of the 8 sky regions, making 32 diffuse foreground parameters in total (group 2 in Table 3). This variation across the sky is an important component of our measurement approach: It is possible to separate the foregrounds from the 21-cm signal because the foregrounds are spectrally smooth while the 21-cm signal has spectral features, and the foregrounds are spatially varying while the 21-cm signal is not (at DARE’s resolution).

The Sun also makes a ~1% contribution to the foregrounds. It is small because it is diluted over the large DARE antenna power pattern. The contribution of the

Table 2
Summary of the planned DARE data analysis procedure.

<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>Combine individual (one-second) spectra to produce calibrated temperature measurements of eight independent regions of the sky</td>
</tr>
<tr>
<td>2.</td>
<td>Utilize Markov Chain Monte Carlo code to fit the data with a model describing the 21-cm global signal, the spatially dependent foregrounds in each sky region, solar system foregrounds, and the overall instrumental response</td>
</tr>
<tr>
<td>3.</td>
<td>Recover the maximum likelihood 21-cm signal, parameterized by its turning points, and the errors on this signal</td>
</tr>
</tbody>
</table>

Fig. 9. Results from a DARE numerical simulation showing confidence regions on frequency and brightness temperature of Turning Points B, C and D for 3000 h of integration, including nominal instrument response and all cosmic foregrounds (Galaxy, discrete extragalactic sources, Sun, Moon). Green and Red regions are 68% and 95% confidence regions, respectively. An ‘x’ marks the input model, while a ‘+’ marks the best fit. The frequency range for Turning Point B is truncated at 40 MHz, since this is the lower limit of the DARE frequency range. Any constraints on the signal below 40 MHz are highly model-dependent, since they are obtained only from the shape of the signal at $\nu > 40$ MHz. For further details, see Harker et al. (2011). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Fig. 10. Extracted signal and 68% confidence limits from a simulated baseline data set compared to the input model. The blue curve shows the input model, the black dot-dashed curve shows the extracted spectrum, and the red dashed lines show the 68% confidence regions on the extracted spectrum. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Table 3
Summary of signal model parameter groups.

<table>
<thead>
<tr>
<th>Model parameter groups</th>
<th>#</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Frequency and amplitude of Turning Points: B, C, D of the 21-cm signal</td>
<td>6</td>
</tr>
<tr>
<td>2. Spectrum of diffuse foregrounds in the 8 different sky regions</td>
<td>32</td>
</tr>
<tr>
<td>3. The shape of the spectrum of the quiet Sun, and its overall normalization in each sky region</td>
<td>11</td>
</tr>
<tr>
<td>4. The temperature and reflectivity of the Moon</td>
<td>2</td>
</tr>
<tr>
<td>5. The instrumental frequency response</td>
<td>22</td>
</tr>
</tbody>
</table>

Sun to each pointing is different, given both its different sky positions as a function of time and possibly varying amplitude as a function of solar cycle, but the spectral shape should remain the same. The quiet Sun has a smooth thermal spectrum, which we describe using the same model as the diffuse foreground. However, $a_1$, $a_2$, and $a_3$ are the same in each sky region, while $T_0$ differs, making a total of 11 parameters (group 3 in Table 3). The Sun can also produce strong (non-thermal) radio bursts. Our approach is not to acquire science data during these relatively short intervals (between a few seconds and up to $\sim 1$ h, Wild et al., 1963), unless the Sun is occluded by the Moon. There are approximately tens of such bursts per year (Gopalswamy et al., 2008), depending on the phase in the solar cycle, and hence they will affect only a small proportion of the mission. Their strength means that bursts can be easily identified, and those data excluded from further processing.

The thermal emission of the Moon enters the back lobe of the antenna, and is described by a single model parameter (the temperature). The Moon also reflects radiation from the sky back towards DARE, and the strength of this reflection is described by one more parameter, making a total of 2 parameters for the properties of the Moon (group 4 in Table 3).

The foreground and signal spectra are modulated by the frequency response of the instrument, giving a final antenna temperature which is well modeled by Eq. (3) (see Fig. 8). The DARE Science Instrument is designed to make the reflection coefficient, $\Gamma$, which is the main quantity determining the frequency response, as smooth as possible, so that the expected spectral smoothness of the foregrounds can be exploited to extract the 21-cm signal (note that the antenna reflection coefficient should not be confused with the parameter describing the reflectivity of the Moon). We assume that $T_c = \varepsilon T_b = \varepsilon T_{rcv}$ and that $\phi_t = 0$ in Eq. (3) for the purposes of this paper, where $\varepsilon$ is a correlation coefficient. It is straightforward, however, to incorporate the general case into the method. We model the amplitude of the reflection coefficient, $|\Gamma(\nu)|$, and the phase term, $\beta(\nu)$, as the ten lowest frequency coefficients of their discrete cosine transform (DCT). This was found to be the lowest number of coefficients which allowed us to model the smallest-scale features of $\Gamma(\nu)$ computed from an electromagnetic model of the antenna. The DCT was chosen as a simple and efficient way of modeling $\Gamma(\nu)$ as a sum of orthogonal functions. It was chosen after some experimentation with various transforms as the one which fit the computed $\Gamma(\nu)$ to reasonable accuracy using a small number of coefficients. Note that use of the DCT does not require the invocation of any special symmetry. Computing the DCT is equivalent to extending the function over a domain twice the original length by attaching a reflected
copy of the function (ensuring the extended function is periodic and even), then computing a Fourier transform. For the Fourier transform, all the coefficients of the sine terms will be zero by construction and so would not need to be stored. Thus, the DCT is merely a special case of a real, discrete Fourier transform, but it allows for simpler book-keeping since the original and transformed arrays are the same length, are real, and contain no redundant information. Along with $e$, and a parameter for the receiver temperature, there are 22 instrumental parameters to be fit (group 5 in Table 3). Although we expect to obtain some independent constraints on these parameters, we assume this provides only weak prior information on their values, and they are all allowed to vary freely in our fitting. Our parameter space therefore has a total of 73 dimensions $(6 + 32 + 11 + 2 + 22)$.

Fig. 9 illustrates that DARE can achieve its science objectives by obtaining the amplitudes and frequencies (redshifts) of the spectral Turning Points with high confidence in the presence of these cosmic foregrounds. This figure shows the 68% and 95% confidence regions on the Turning Point parameters, after marginalizing over the nuisance parameters (i.e., those of the foregrounds and instrument).

### 5.2. Other potential contributions

Other processes have a minor effect on the spectrum. As DARE orbits the Moon, dust particles from the lunar exosphere impact the antenna. The plasma formed by these impacts generates an antenna response (e.g., Meyer-Vernet, 1985), which also constitutes a weak foreground. The resulting spectrum is estimated from models of the dust distribution around the Moon (e.g., Stubbs et al., 2010), and from the velocity, altitude, and surface area of DARE. Fig. 12 shows that the dust foreground is negligible for DARE.

The plasma that composes the interplanetary medium in the lunar neighborhood radiates at frequencies well below the DARE band (e.g., plasma shot noise). Most of these plasma effects produce radio emission near the plasma frequency which is typically $<100$ kHz for the solar wind (e.g., Kasaba et al. 2000; Stenzel 1989). Auroral Kilometric Radiation (AKR), generated by cyclotron emission from electrons spiraling within the Earth’s magnetic field, produces emissions at frequencies 50–500 kHz (e.g., Ergun et al., 1998). Thus, local plasma effects in the Moon-Earth environment will not contribute to DARE’s foreground.

Jupiter is also a radio source, but its amplitude is of order $10^{-4}$ that of the Sun (e.g., Zarka, 2004), so at present it is not explicitly included in our modeling.

---

**Fig. 11.** Sky map at 70 MHz derived from the global sky model of de Oliveira-Costa et al. (2008). The Galactic plane is clearly visible as the intense area near the center of the map. The white contours show the power response of a crossed dipole antenna (contours spaced at 10% of maximum).

**Fig. 12.** Comparison of the 21-cm signal with various foregrounds. The contribution of the Galaxy is shown for a patch of sky away from the Galactic center; the reflected signal shows the magnitude of this emission after being reflected by the Moon and received through the backlobe of the antenna, which suppresses its relative contribution. Thermal radiation from the Moon is also suppressed by entering through the backlobe. The Galaxy and the Sun dwarf the 21-cm signal (shown as a red solid line when in emission, and red dashed for absorption). The blue solid curve shows thermal noise for 1000 h of integration, while the blue dotted curve shows this with addition of a residual of 1 mK. The noise spectrum caused by dust impacts is negligible. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

---

Table 4
Redshifts (z) and frequencies (ν) of turning points in our reference model, and uncertainties in (z,ν) after 3000 h of integration. Uncertainties are derived from a model of the extraction process in the presence of foregrounds, thermal noise and instrumental corruption (Section 5). The upper and lower bounds given are at the 95% confidence level.

<table>
<thead>
<tr>
<th>Turning Points</th>
<th>True position</th>
<th>3000 h</th>
<th>Lower (upper) bound</th>
<th>Best-fit</th>
<th>Upper (lower) bound</th>
<th>% Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>B</td>
<td>z</td>
<td>29.74</td>
<td>28.63</td>
<td>30.12</td>
<td>34.16</td>
<td>8.3</td>
</tr>
<tr>
<td></td>
<td>ν (MHz)</td>
<td>(46.20)</td>
<td>(47.96)</td>
<td>(45.65)</td>
<td>(40.40)</td>
<td>(9.2)</td>
</tr>
<tr>
<td>C</td>
<td>z</td>
<td>20.75</td>
<td>20.59</td>
<td>20.85</td>
<td>21.16</td>
<td>1.4</td>
</tr>
<tr>
<td></td>
<td>ν (MHz)</td>
<td>(65.30)</td>
<td>(65.78)</td>
<td>(65.00)</td>
<td>(64.09)</td>
<td>(1.3)</td>
</tr>
<tr>
<td>D</td>
<td>z</td>
<td>13.29</td>
<td>13.22</td>
<td>13.27</td>
<td>13.32</td>
<td>0.4</td>
</tr>
<tr>
<td></td>
<td>ν (MHz)</td>
<td>(99.40)</td>
<td>99.86</td>
<td>(99.53)</td>
<td>(99.20)</td>
<td>(0.3)</td>
</tr>
</tbody>
</table>

In addition to these spectrally smooth foregrounds, carbon atoms in the Galaxy produce radio recombination lines (RRLs, Pritchard and Loeb, 2010). These lines are sharp (∼10 kHz wide), but spaced at known intervals of about 1 MHz. Any spectral channels containing RRLs will need to be discarded before combining the one-second spectra to make the integrated spectra. The discarded channels will constitute a very small fraction of DARE’s bandwidth and so their excision will have only a minor effect on the level of noise in the final spectra.

DARE’s placement in a lunar orbit allows it to access the RFI shielded zone above the lunar farside so that it does not have to contend with human-generated RFI. However, spacecraft at the Earth–Sun L2 point could potentially reflect terrestrial (or solar) emissions at a level that would vitiate DARE’s intended measurements. We estimate that any such reflections are, in fact, not likely to constitute a problem. For example, reflection of RFI off the JWST sunshade is calculated to be 10^{-7} that of the thermal noise in Fig. 12.

6. Constraints on the epochs of first star and black hole formation from DARE observations

Accurate constraints on Turning Point B are the most challenging because of the brighter foregrounds (Fig. 12) and diminished instrument sensitivity (Fig. 8) at lower frequencies. But, Turning Point B is important because it marks the epoch of first star formation and it will be the most difficult to constrain by any other method or mission. The DARE synthetic observation modeling (Section 5) was used to estimate the uncertainties in the redshifts in the redshifts and frequencies of all three Turning Points shown in Table 4. For 3000 h of integration, we obtain a tight (∼10% of the true value) measurement of the frequency and redshift of Turning Point B. The redshifts of Turning Points C (first accreting black holes) and D (beginning of Epoch of Reionization) can be measured with small uncertainties of only ±1.4% and ±0.4%, respectively, at the 95% confidence level in this integration time.

With a 200 km altitude lunar orbit, the orbital period is 127 min, during which the DARE spacecraft will be out of direct line-of-sight of the Earth for 45 min. Diffraction effects around the lunar limb reduce the useful science collection time. For the RFI to be attenuated below the expected science signal (>100 dB), the effective collection time is reduced to approximately 30 min, consistent with experience from RAE-2 and the Apollo VHF communication system. Modeling of the thermal load of the Science Instrument as it moves in and out of sunlight above the far-side indicates that no more than about 5 min is lost due to thermal relaxation. To be conservative, we adopt a science collection time of 15 min per orbit. With this conservative collection time, the baseline mission lifetime is 3 years in order to obtain 3000 h of integration, from which the level of uncertainties in Table 4 is achieved.

7. Summary

The Dark Ages Radio Explorer (DARE) is a space mission concept that will probe for the first time the epoch in the early Universe which begins with the Dark Ages and leads to the Cosmic Dawn when the first stars, galaxies, and black holes were born. DARE will make unique observations of the highly redshifted 21-cm signal from the hyperfine transition of neutral hydrogen arising from the intergalactic medium. The sky-averaged spectrum is theoretically expected to contain features, which we term “Turning Points”, that correspond to the redshifts (epochs) when the first stars were formed, when the first accreting black holes turned on, and when the Universe began its last phase transition from neutral to ionized hydrogen (Epoch of Reionization). DARE is proposed to orbit the Moon and to take data only above the radio-quiet lunar farside, the ideal environment for such observations. The science instrument is composed of a three component radiometer that includes a pair of bi-conical, tapered, electrically-short dipole antennas, along with a receiver and a digital spectrometer. A key feature of DARE is the calibration and foreground removal approach, derived from experience with the ground-based pathfinder EDGES, using differential spectral radiometry and a Markov Chain Monte Carlo maximum likelihood analysis tool similar to the approach used for observations of the Cosmic Microwave Background.
Acknowledgements

The authors would like to thank the management of the NASA Ames Research Center (ARC) for their strong support and investment in the DARE concept, especially ARC Director P. Worden along with P. Klupar, B.J. Jaroux, as well as NASA Lunar Science Institute (NSLI) Director Y. Pendleton and NSLI Deputy Director G. Schmidt. We are particularly grateful to L. Webster, J. Bauman, H. Sanchez, D. Santiago, T. Soderman, and J. Baer at ARC, as well as I. O'Dwyer, A. Tanner, and R. Jarnot at JPL. We would like to acknowledge Ball Aerospace and, especially, L. Hardaway for their investment of resources and effort on the DARE concept. This concept was conceived and supported by the Lunar University Network for Astrophysics Research (LUNAR) (http://lunar.colorado.edu), headquartered at the University of Colorado Boulder, funded by the NSLI via Cooperative Agreement NNA09DB30A. Part of this research was conducted at the Jet Propulsion Laboratory, California Institute of Technology, under contract to the National Aeronautics and Space Administration.

References


